

Unit 8 Solving Equations & Inequalities

8.0 Equation Solving With Integers

Recall: To **solve** an equation means to find the value of the variable which satisfies the equation
[Reviewed in 7.0 already]

Ex. Solve: $2x + 6 = 20$

$$\begin{array}{r} -6 \quad -6 \\ 2x + 6 = 20 \\ \hline 2x = 14 \\ \hline \frac{2x}{2} = \frac{14}{2} \\ \hline x = 7 \end{array}$$

★ isolate the variable
★ opposite operations on both sides
★ SAMDEB

Equations with Variable on Both Sides

Ex. Solve:

a) $8x = 3x - 15$
 ~~$-3x$~~ ~~$-3x$~~

$$\begin{array}{r} 5x = -15 \\ \hline \frac{5x}{5} = \frac{-15}{5} \\ \hline x = -3 \end{array}$$

★ isolate variable terms from constant terms

b) $6x - 5 = 2x + 7$
 ~~$-2x$~~ ~~$+5$~~ ~~$-2x$~~ ~~$+5$~~

$$\begin{array}{r} 4x = 12 \\ \hline \frac{4x}{4} = \frac{12}{4} \\ \hline x = 3 \end{array}$$

c) $-5 - 8t = -9t - 7$
 ~~$+7$~~ ~~$+8t$~~ ~~$+8t$~~ ~~$+7$~~

$$\begin{array}{r} 2 = -t \\ \hline \frac{2}{-1} = \frac{-t}{-1} \\ \hline -2 = t \end{array}$$

d) $-5m - 2 = 3m - 2$
 ~~$+5m$~~ ~~$+2$~~ ~~$+5m$~~ ~~$+2$~~

$$\begin{array}{r} 0 = 8m \\ \hline \frac{0}{8} = \frac{8m}{8} \\ \hline 0 = m \end{array}$$

e) $z - 2 = 2z - 4$
 ~~$-z$~~ ~~$+4$~~ ~~-2~~ ~~$+4$~~

$$\begin{array}{r} 2 = 2 \\ \hline \frac{2}{1} = \frac{2}{1} \\ \hline 2 = 2 \end{array}$$

★
 $-2 = 5$
 $2 = -5$
 $-6 = -8$
 $6 = 8$

Unsimplified Equations

Ex. Solve:

a) $3(a-3) + 7 = 5a - 8 - 4a$

$$3a - 9 + 7 = a - 8$$

$$3a - 2 = a - 8$$
$$-a + 2 \quad -a + 2$$

$$\frac{2a}{2} = \frac{-6}{2}$$

$$\boxed{a = -3}$$

b) $7 - 3(5t - 10) = 67$

$$7 - 15t + 30 = 67$$

$$-15t + 37 = 67$$
$$-37 \quad -37$$

$$-15t = 30$$
$$\frac{-15t}{-15} = \frac{30}{-15}$$

$$\boxed{t = -2}$$

* simplify each side first
↳ distribute, like terms

c) $6p - 1(5p + 5) = -8 - 2(p + 12)$

$$6p - 5p - 5 = -8 - 2p - 24$$

$$p - 5 = -2p - 32$$
$$+2p + 5 \quad +2p + 5$$

$$\frac{3p}{3} = \frac{-27}{3}$$

$$\boxed{p = -9}$$