

Unit 8 Solving Equations & Inequalities

8.1 One-Step Equations

- Equation solving with rational (fraction or decimal) coefficients.

1. Solving $ax = b$

Ex. Solve:

$$a) \cancel{3}x = -\frac{2}{3}$$

$$x = -\frac{2}{3} \times \frac{1}{3}$$

$$\boxed{x = -\frac{2}{9}}$$

$$b) \cancel{2}x = \frac{3}{4}$$

$$x = \frac{3}{4} \times \frac{1}{2}$$

$$\boxed{x = \frac{3}{8}}$$

$$c) -2\frac{1}{2}k = -3\frac{1}{2}$$

$$\cancel{-5}k = \frac{-7}{2}$$

$$\cancel{-5}k = \frac{-7}{2}$$

$$k = \frac{-7}{2} \times \frac{2}{5} = \boxed{\frac{-7}{5}} = \boxed{-1\frac{2}{5}}$$

★ improper fractions

$$d) \cancel{5.5}b = -3.41$$

$$\boxed{b = -0.62}$$

Ex. A store sells mitts at 30% off the regular price. If the sale price was \$34.99 find the regular price.

let x = regular price $\rightarrow 70\%$ of the regular price = sale price

$$\downarrow$$

$$\frac{0.7x}{0.7} = \frac{34.99}{0.7}$$

$$\boxed{x = \$49.99}$$

2. Solving $\frac{x}{a} = b$

Ex. Solve:

$$a) \frac{m}{3} = -\frac{2}{5}$$

$$\times 3 \quad \times 3$$

$$m = -\frac{2}{5} \times \frac{3}{1}$$

$$\boxed{m = -\frac{6}{5}}$$

$$b) \frac{x}{2} = \left(\frac{5}{6}\right) \frac{2}{1}$$

$$\boxed{x = \frac{5}{3}}$$

$$c) \left(\frac{u}{1.3}\right) = (0.8)^{1.3}$$

$$\boxed{u = 1.04}$$

3. Solving $\frac{a}{x} = b$

Ex. Solve:

$$a) \left(\frac{136.68}{m} \right) = (13.4) m$$

$$\frac{136.68}{13.4} = \frac{13.4 m}{13.4}$$

$$\boxed{10.2 = m}$$

$$b) \left(\frac{4}{5} \right) = \left(\frac{-3}{2x} \right) \quad \cancel{2x}$$

$$\frac{8x}{5} = \frac{-3}{5}$$

$$x = \frac{-3}{1} \times \frac{5}{8}$$

$$x = \frac{-15}{8}$$

Ex. The formula for speed, s , is $S = \frac{d}{t}$ where d is distance and t is time. If a dogsled team averages a speed of 23.5 km/h, how long will it take to complete a 50 km circuit (nearest tenth)?

$$S = \frac{d}{t}$$

$$t (23.5) = \left(\frac{50}{t} \right) t$$

$$\frac{23.5t}{23.5} = \frac{50}{23.5}$$

$$t = \boxed{2.1 \text{ hours}}$$